

Linearfaktoren

Bestimme die Funktionsvorschrift in der Produktdarstellung und multipliziere dann aus.

Lösung

1) $x_1 : +3 \quad x_2 : -2 \quad x_3 : -1$

$$\begin{aligned} f(x) &= (x + 3) \cdot (x - 2) \cdot (x - 1) \\ f(x) &= (x^2 - 2x + 3x - 6) \cdot (x - 1) \\ f(x) &= (x^3 - 1x^2 - 2x^2 + 2x + 3x^2 - 3x - 6x + 6) \\ f(x) &= x^3 + 0x^2 - 7x + 6 \end{aligned}$$

2) $x_1 : -3 \quad x_2 : +1 \quad x_3 : -2$

$$\begin{aligned} f(x) &= (x - 3) \cdot (x + 1) \cdot (x - 2) \\ f(x) &= (x^2 + 1x - 3x - 3) \cdot (x - 2) \\ f(x) &= (x^3 - 2x^2 + 1x^2 - 2x - 3x^2 + 6x - 3x + 6) \\ f(x) &= x^3 - 4x^2 + 1x + 6 \end{aligned}$$

3) $x_1 : +3 \quad x_2 : -1 \quad x_3 : -2$

$$\begin{aligned} f(x) &= (x + 3) \cdot (x - 1) \cdot (x - 2) \\ f(x) &= (x^2 - 1x + 3x - 3) \cdot (x - 2) \\ f(x) &= (x^3 - 2x^2 - 1x^2 + 2x + 3x^2 - 6x - 3x + 6) \\ f(x) &= x^3 + 0x^2 - 7x + 6 \end{aligned}$$

4) $x_1 : +1 \quad x_2 : +6 \quad x_3 : +2$

$$\begin{aligned} f(x) &= (x + 1) \cdot (x + 6) \cdot (x + 2) \\ f(x) &= (x^2 + 6x + 1x + 6) \cdot (x + 2) \\ f(x) &= (x^3 + 2x^2 + 6x^2 + 12x + 1x^2 + 2x + 6x + 12) \\ f(x) &= x^3 + 9x^2 + 20x + 12 \end{aligned}$$

5) $x_1 : +2 \quad x_2 : +5 \quad x_3 : +6$

$$\begin{aligned} f(x) &= (x + 2) \cdot (x + 5) \cdot (x + 6) \\ f(x) &= (x^2 + 5x + 2x + 10) \cdot (x + 6) \\ f(x) &= (x^3 + 6x^2 + 5x^2 + 30x + 2x^2 + 12x + 10x + 60) \\ f(x) &= x^3 + 13x^2 + 52x + 60 \end{aligned}$$

6) $x_1 : +6 \quad x_2 : -1 \quad x_3 : -8$

$$\begin{aligned} f(x) &= (x + 6) \cdot (x - 1) \cdot (x - 8) \\ f(x) &= (x^2 - 1x + 6x - 6) \cdot (x - 8) \\ f(x) &= (x^3 - 8x^2 - 1x^2 + 8x + 6x^2 - 48x - 6x + 48) \\ f(x) &= x^3 - 3x^2 - 46x + 48 \end{aligned}$$

7) $x_1 : +9 \quad x_2 : +6 \quad x_3 : +2$

$$\begin{aligned} f(x) &= (x + 9) \cdot (x + 6) \cdot (x + 2) \\ f(x) &= (x^2 + 6x + 9x + 54) \cdot (x + 2) \\ f(x) &= (x^3 + 2x^2 + 6x^2 + 12x + 9x^2 + 18x + 54x + 108) \\ f(x) &= x^3 + 17x^2 + 84x + 108 \end{aligned}$$

8) $x_1 : +9 \quad x_2 : -5 \quad x_3 : +6$

$$\begin{aligned} f(x) &= (x + 9) \cdot (x - 5) \cdot (x + 6) \\ f(x) &= (x^2 - 5x + 9x - 45) \cdot (x + 6) \\ f(x) &= (x^3 + 6x^2 - 5x^2 - 30x + 9x^2 + 54x - 45x - 270) \\ f(x) &= x^3 + 10x^2 - 21x - 270 \end{aligned}$$