

## Linearfaktoren

Bestimme die Funktionsvorschrift in der Produktdarstellung und multipliziere dann aus.

### Lösung

1)  $x_1 : +2 \quad x_2 : +4 \quad x_3 : -3$

$$\begin{aligned} f(x) &= (x+2) \cdot (x+4) \cdot (x-3) \\ f(x) &= (x^2 + 4x + 2x + 8) \cdot (x-3) \\ f(x) &= (x^3 - 3x^2 + 4x^2 - 12x + 2x^2 - 6x + 8x - 24) \\ f(x) &= x^3 + 3x^2 - 10x - 24 \end{aligned}$$

2)  $x_1 : +2 \quad x_2 : +3 \quad x_3 : +1$

$$\begin{aligned} f(x) &= (x+2) \cdot (x+3) \cdot (x+1) \\ f(x) &= (x^2 + 3x + 2x + 6) \cdot (x+1) \\ f(x) &= (x^3 + 1x^2 + 3x^2 + 3x + 2x^2 + 2x + 6x + 6) \\ f(x) &= x^3 + 6x^2 + 11x + 6 \end{aligned}$$

3)  $x_1 : +1 \quad x_2 : +3 \quad x_3 : +4$

$$\begin{aligned} f(x) &= (x+1) \cdot (x+3) \cdot (x+4) \\ f(x) &= (x^2 + 3x + 1x + 3) \cdot (x+4) \\ f(x) &= (x^3 + 4x^2 + 3x^2 + 12x + 1x^2 + 4x + 3x + 12) \\ f(x) &= x^3 + 8x^2 + 19x + 12 \end{aligned}$$

4)  $x_1 : +2 \quad x_2 : +6 \quad x_3 : -1$

$$\begin{aligned} f(x) &= (x+2) \cdot (x+6) \cdot (x-1) \\ f(x) &= (x^2 + 6x + 2x + 12) \cdot (x-1) \\ f(x) &= (x^3 - 1x^2 + 6x^2 - 6x + 2x^2 - 2x + 12x - 12) \\ f(x) &= x^3 + 7x^2 + 4x - 12 \end{aligned}$$

5)  $x_1 : +6 \quad x_2 : +7 \quad x_3 : +3$

$$\begin{aligned} f(x) &= (x+6) \cdot (x+7) \cdot (x+3) \\ f(x) &= (x^2 + 7x + 6x + 42) \cdot (x+3) \\ f(x) &= (x^3 + 3x^2 + 7x^2 + 21x + 6x^2 + 18x + 42x + 126) \\ f(x) &= x^3 + 16x^2 + 81x + 126 \end{aligned}$$

6)  $x_1 : -7 \quad x_2 : -1 \quad x_3 : -3$

$$\begin{aligned} f(x) &= (x-7) \cdot (x-1) \cdot (x-3) \\ f(x) &= (x^2 - 1x - 7x + 7) \cdot (x-3) \\ f(x) &= (x^3 - 3x^2 - 1x^2 + 3x - 7x^2 + 21x + 7x - 21) \\ f(x) &= x^3 - 11x^2 + 31x - 21 \end{aligned}$$

7)  $x_1 : +10 \quad x_2 : -1 \quad x_3 : -9$

$$\begin{aligned} f(x) &= (x+10) \cdot (x-1) \cdot (x-9) \\ f(x) &= (x^2 - 1x + 10x - 10) \cdot (x-9) \\ f(x) &= (x^3 - 9x^2 - 1x^2 + 9x + 10x^2 - 90x - 10x + 90) \\ f(x) &= x^3 + 0x^2 - 91x + 90 \end{aligned}$$

8)  $x_1 : -5 \quad x_2 : -8 \quad x_3 : +3$

$$\begin{aligned} f(x) &= (x-5) \cdot (x-8) \cdot (x+3) \\ f(x) &= (x^2 - 8x - 5x + 40) \cdot (x+3) \\ f(x) &= (x^3 + 3x^2 - 8x^2 - 24x - 5x^2 - 15x + 40x + 120) \\ f(x) &= x^3 - 10x^2 + 1x + 120 \end{aligned}$$