

Linearfaktoren

Bestimme die Funktionsvorschrift in der Produktdarstellung und multipliziere dann aus.

Lösung

1) $x_1 : +4 \quad x_2 : +2 \quad x_3 : -1$

$$\begin{aligned} f(x) &= (x+4) \cdot (x+2) \cdot (x-1) \\ f(x) &= (x^2 + 2x + 4x + 8) \cdot (x-1) \\ f(x) &= (x^3 - 1x^2 + 2x^2 - 2x + 4x^2 - 4x + 8x - 8) \\ f(x) &= x^3 + 5x^2 + 2x - 8 \end{aligned}$$

2) $x_1 : -2 \quad x_2 : +4 \quad x_3 : +3$

$$\begin{aligned} f(x) &= (x-2) \cdot (x+4) \cdot (x+3) \\ f(x) &= (x^2 + 4x - 2x - 8) \cdot (x+3) \\ f(x) &= (x^3 + 3x^2 + 4x^2 + 12x - 2x^2 - 6x - 8x - 24) \\ f(x) &= x^3 + 5x^2 - 2x - 24 \end{aligned}$$

3) $x_1 : +5 \quad x_2 : -2 \quad x_3 : +1$

$$\begin{aligned} f(x) &= (x+5) \cdot (x-2) \cdot (x+1) \\ f(x) &= (x^2 - 2x + 5x - 10) \cdot (x+1) \\ f(x) &= (x^3 + 1x^2 - 2x^2 - 2x + 5x^2 + 5x - 10x - 10) \\ f(x) &= x^3 + 4x^2 - 7x - 10 \end{aligned}$$

4) $x_1 : -6 \quad x_2 : -2 \quad x_3 : -5$

$$\begin{aligned} f(x) &= (x-6) \cdot (x-2) \cdot (x-5) \\ f(x) &= (x^2 - 2x - 6x + 12) \cdot (x-5) \\ f(x) &= (x^3 - 5x^2 - 2x^2 + 10x - 6x^2 + 30x + 12x - 60) \\ f(x) &= x^3 - 13x^2 + 52x - 60 \end{aligned}$$

5) $x_1 : -3 \quad x_2 : +1 \quad x_3 : +6$

$$\begin{aligned} f(x) &= (x-3) \cdot (x+1) \cdot (x+6) \\ f(x) &= (x^2 + 1x - 3x - 3) \cdot (x+6) \\ f(x) &= (x^3 + 6x^2 + 1x^2 + 6x - 3x^2 - 18x - 3x - 18) \\ f(x) &= x^3 + 4x^2 - 15x - 18 \end{aligned}$$

6) $x_1 : -8 \quad x_2 : -5 \quad x_3 : -2$

$$\begin{aligned} f(x) &= (x-8) \cdot (x-5) \cdot (x-2) \\ f(x) &= (x^2 - 5x - 8x + 40) \cdot (x-2) \\ f(x) &= (x^3 - 2x^2 - 5x^2 + 10x - 8x^2 + 16x + 40x - 80) \\ f(x) &= x^3 - 15x^2 + 66x - 80 \end{aligned}$$

7) $x_1 : +4 \quad x_2 : -10 \quad x_3 : -1$

$$\begin{aligned} f(x) &= (x+4) \cdot (x-10) \cdot (x-1) \\ f(x) &= (x^2 - 10x + 4x - 40) \cdot (x-1) \\ f(x) &= (x^3 - 1x^2 - 10x^2 + 10x + 4x^2 - 4x - 40x + 40) \\ f(x) &= x^3 - 7x^2 - 34x + 40 \end{aligned}$$

8) $x_1 : +8 \quad x_2 : +7 \quad x_3 : -2$

$$\begin{aligned} f(x) &= (x+8) \cdot (x+7) \cdot (x-2) \\ f(x) &= (x^2 + 7x + 8x + 56) \cdot (x-2) \\ f(x) &= (x^3 - 2x^2 + 7x^2 - 14x + 8x^2 - 16x + 56x - 112) \\ f(x) &= x^3 + 13x^2 + 26x - 112 \end{aligned}$$